

Name: _____

Key

MATH 173 Unit Exam 3

*Show All Work
Justify All Conclusions
No Graphing Calculators Allowed*

Dazzle Me

Instructor: Grøndahl

- 1) Estimate the period of
- g

z	1	11	21	31	41	51	61	71	81
$g(z)$	5	3	2	3	5	3	2	3	5

$$p = 41 - 1 = 40$$

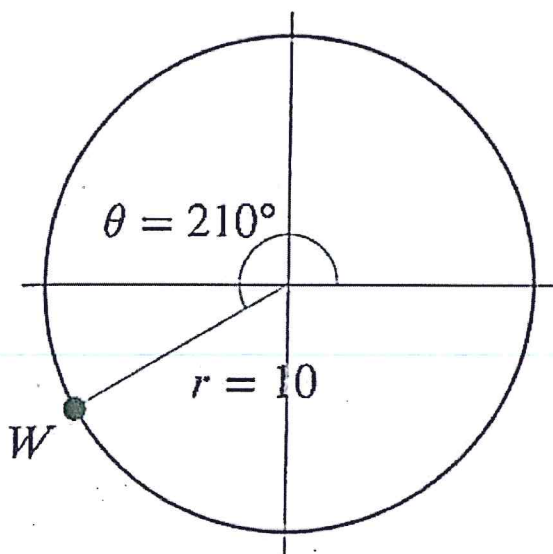
- 2) Give the reference angle for the angle
- 100°

$$\theta_{\text{REF}} = 80^\circ$$

- 3) What angle in radians corresponds to -2 rotations around the unit circle?

$$\theta = -2(2\pi) = -4\pi$$

- 4) Find the exact values for the coordinates of point
- W

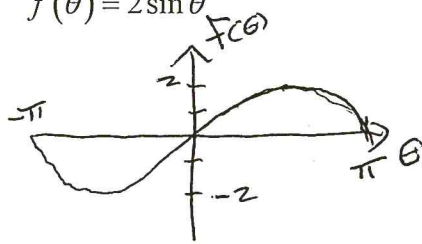


$$x = r \cos \theta = 10 \cos 210^\circ = 10 \left(-\frac{\sqrt{3}}{2} \right) = -5\sqrt{3}$$

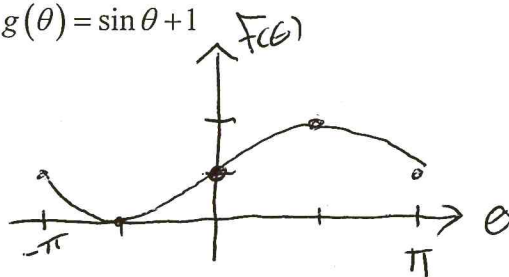
$$y = r \sin \theta = 10 \sin 210^\circ = 10 \left(-\frac{1}{2} \right) = -5$$

5) Graph the following functions and determine if the function is odd or not.

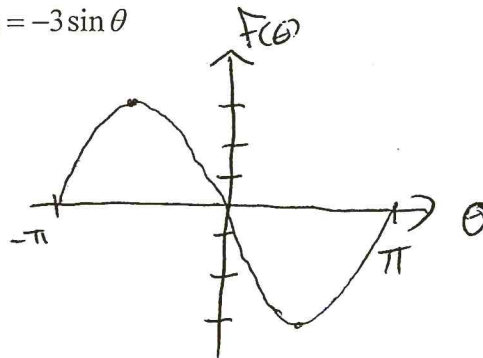
a. $f(\theta) = 2 \sin \theta$



b. $g(\theta) = \sin \theta + 1$



c. $h(\theta) = -3 \sin \theta$



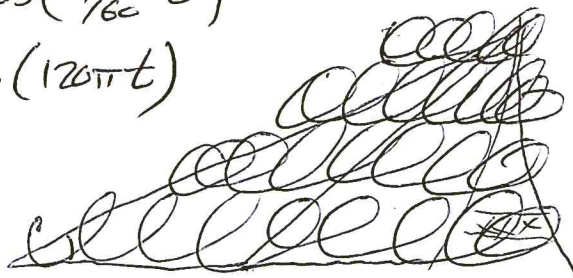
6) Household electrical power in the US is provided in the form of alternating current. Typically the voltage cycles smoothly between +155.6 volts and -155.6 volts 60 times per second. Use a sinusoidal function to model voltage, V , as a function of time, t , in seconds since the voltage was at its peak.

$$V(t) = 155.6 \cos\left(\frac{2\pi}{1/60} t\right)$$

$$= 155.6 \cos(120\pi t)$$

$$f = 60$$

$$p = 1/60$$

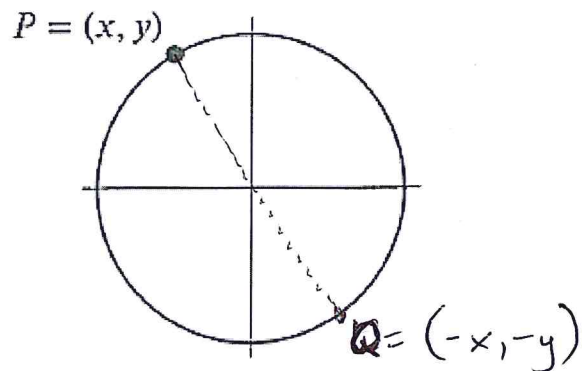


- 7) Find the slope of the line perpendicular to the line, l , passing through the origin at an angle of 35° .

$$\text{SLOPE OF } l : m = \tan 35^\circ$$

$$\text{SLOPE OF } \perp : m = \frac{-1}{\tan 35^\circ}$$

- 8) Using the unit circle below where the point P corresponds to an angle of t radians,



- a. What are the coordinates of the point Q corresponding to the angle $t + \pi$

$$Q = (-x, -y)$$

- b. Show that $\cos(t + \pi) = -\cos t$

$$\cos(t) = x \text{ COORDINATE OF } P$$

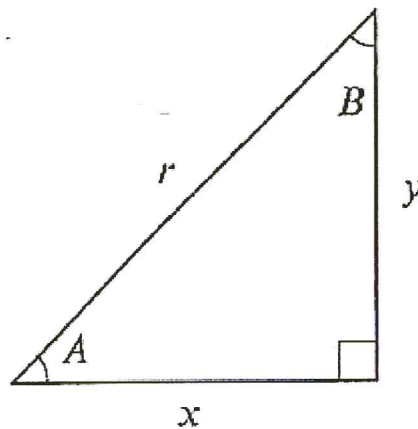
$$\cos(t + \pi) = x \text{ COORDINATE OF } Q$$

$$\therefore \cos(t + \pi) = -\cos(t)$$

9) Solve $\tan t = \sqrt{3}$, $0 \leq t \leq 2\pi$

$$t = \frac{\pi}{3}, \frac{4\pi}{3}$$

10) Find the value of A , r , and y , given that $B = 77^\circ$ and $x = 9$



$$A = 90^\circ - B = 90^\circ - 77^\circ = 13^\circ$$

$$\tan B = \frac{x}{y}$$

$$y = \frac{9}{\tan 77^\circ}$$

$$\sin B = \frac{x}{r}$$

$$\sin 77^\circ = \frac{9}{r}$$

$$r = \frac{9}{\sin 77^\circ}$$

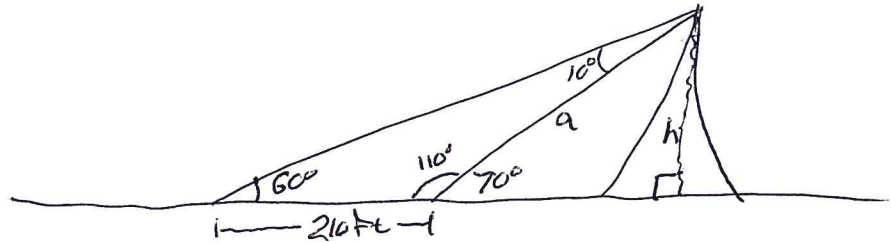
~~$$r = \frac{9}{\sin 77^\circ}$$~~

~~$$y = \frac{9}{\tan 77^\circ}$$~~

- 11) To measure the height of the Eiffel Tower in Paris, a person stands away from the base and measure the angle of elevation to the top of the tower to be 60° . Moving 210 ft. closer, the angle of elevation to the top of the tower is 70° . How tall is the Eiffel Tower?

$$\frac{\sin 60^\circ}{a} = \frac{\sin 10^\circ}{210}$$

$$a = \frac{210 \sin 60^\circ}{\sin 10^\circ}$$

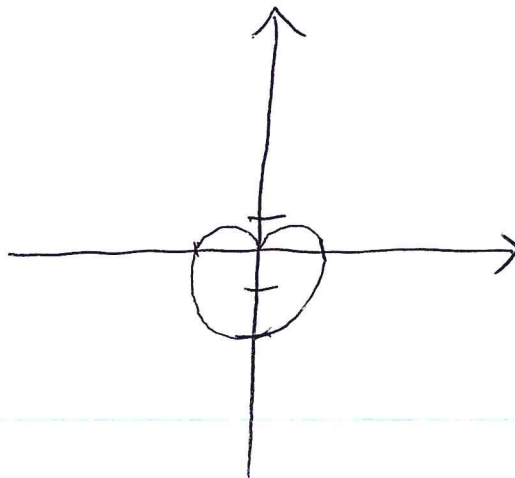


$$\sin 70^\circ = \frac{h}{a}$$

$$h = a \sin 70^\circ = \frac{210 \sin 60^\circ \sin 70^\circ}{\sin 10^\circ}$$

- 12) Sketch a graph of the polar equation $r = 1 - \sin \theta$

r	θ
1	0
0	$\pi/2$
1	π
2	$3\pi/2$
0	2π



13) Solve $\cos(2t) = \frac{1}{2}$

$$2t = \pm \frac{\pi}{3} + 2\pi k$$

$$t = \pm \frac{\pi}{6} + \pi k$$

14) Simplify $\frac{\cos \phi - 1}{\sin \phi} + \frac{\sin \phi}{\cos \phi + 1}$

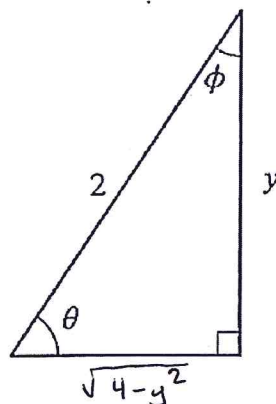
$$= \frac{(\cos \phi - 1)(\cos \phi + 1)}{\sin \phi (\cos \phi + 1)} + \frac{\sin^2 \phi}{\sin \phi (\cos \phi + 1)}$$

$$= \frac{\cos^2 \phi - 1 + \sin^2 \phi}{\sin \phi (\cos \phi + 1)}$$

$$= \frac{1 - 1}{\sin \phi (\cos \phi + 1)}$$

$$= 0$$

15) Find a simplified expression for the following in terms of y



a. $\cos(\theta - \phi)$

$$\begin{aligned} & \cos\theta \cos\phi + \sin\theta \sin\phi \\ &= \left(\frac{\sqrt{4-y^2}}{2}\right)\left(\frac{y}{2}\right) + \left(\frac{y}{2}\right)\left(\frac{\sqrt{4-y^2}}{2}\right) \\ &= \frac{y\sqrt{4-y^2}}{2} \end{aligned}$$

b. $\sin(\theta + \phi)$

$$\begin{aligned} &= \sin(90^\circ) \\ &= \underline{1} \end{aligned}$$

16) Use DeMoivre's Thm. to evaluate $\left(\cos\frac{2\pi}{3} + i\sin\frac{2\pi}{3}\right)^3$

$$\begin{aligned} &= \left(-\frac{1}{2} + i\frac{\sqrt{3}}{2}\right)^3 & r &= 1 \\ & & \theta &= \frac{2\pi}{3} \\ &= \left(e^{i\frac{2\pi}{3}}\right)^3 \\ &= e^{2\pi i} \\ &= \cos 2\pi + i\sin 2\pi \\ &= 1 \end{aligned}$$

